PAKTURK 12th National Interschool Math Olympiad

Q1: Which of the following numbers is **<u>not</u>** an integer?

A)
$$\frac{2016}{6}$$
 B) $\frac{2015}{5}$ C) $\frac{2014}{4}$ D) $\frac{2013}{3}$

Solution:
A)
$$\frac{2016}{6} = 336$$
 B) $\frac{2015}{5} = 403$
C) $\frac{2014}{4} = 503.5$ D) $\frac{2013}{3} = 671$

Answer: C

D) 4

Q2:
$$3+2\times[(-5+2)-(-7+3)]-4=?$$

A) 0 C) 2 <mark>B) 1</mark>

Solution:

$$3+2\times[(-5+2)-(-7+3)]-4 =$$

 $\Rightarrow 3+2\times[(-3)-(-4)]-4 =$
 $\Rightarrow 3+2\times1-4=5-4=1$
Answer: B
Q3: Evaluate $\frac{2}{3} + \frac{3}{3} =$
A) $\frac{3}{2}$ B) $\frac{7}{3}$ C) $\frac{3}{5}$ D) $\frac{4}{5}$

Solution:

$$\frac{\frac{2}{3}}{\frac{2}{2}} + \frac{3}{\frac{3}{2}} = \frac{2}{3} \times \frac{1}{2} + 3 \times \frac{2}{3} = \frac{1}{3} + 2 = \frac{1+6}{3} = \frac{7}{3}$$
Answer: B

Q4:
$$\frac{1}{2} + \frac{1}{3} \div \left(\frac{1}{2} + \frac{1}{3}\right)_{=}{=} ?$$

A) $\frac{1}{5}$ B) $\frac{3}{2}$ C) $\frac{3}{5}$ D) $\frac{9}{4}$
Solution:
 $\frac{1}{2} + \frac{1}{3} \div \left(\frac{1}{2} + \frac{1}{3}\right)_{=}{=} \frac{1}{2} + \frac{1}{3} \div \frac{5}{6}_{=}{=} \frac{1}{2} + \frac{1}{3} \div \frac{6}{5}_{=}{=} \frac{1}{0.4}$
 $\frac{1}{2} + \frac{2}{5}_{=}{=} \frac{9}{10} \div \frac{4}{10} = \frac{9}{10} \times \frac{10}{4} = \frac{9}{4}$
Q5: 14391 ÷ 13 = ?
A) 1107 B) 1161 C) 1071 D) 1171
Solution: 14391 ÷ 13 = 1107
Answer: A
Q6: Which of the following is smaller than $\frac{6}{5}$?
A) 1.15 B) 1.20 C) 1.25 D) 1.30
Solution:
 $\frac{6}{5} = 1.2 > 1.15$

Solution:

$$\frac{6}{5} = 1.2 \rangle 1.15$$
Answer: A

Q7:
$$\frac{1}{\frac{0.1}{0.11} + \frac{0.3}{0.33} - \frac{0.6}{0.66}} = ?$$

A) $\frac{11}{3}$ B) $\frac{11}{6}$ C) $\frac{11}{10}$ D) $\frac{6}{11}$

						An	swer: C	
	0.11	0.33	0.66	11	11	11		
Solution:	0.1	0.3	0.6	10	10	10	$-\frac{10}{10}$	
Solution		1	-	_	1	-	_ 11	

Q8:	Find the value of x in the equation
$4x + \frac{1}{2}$	$\left(3x-2\right)=\frac{9}{2}x.$

A) 1 B) 2 C) 3 D) 4

Solution: $4x + \frac{1}{2}(3x - 2) = \frac{9}{2}x \Rightarrow \frac{8x + 3x - 2}{2} = \frac{9x}{2}$ $\Rightarrow 11x - 2 = 9x \Rightarrow 2x = 2 \Rightarrow x = 1$ Answer: A

a-b=1 **Q9:** What is the value of 3a+c if a+c=7? b-c=2

A) 8 B) 11



Q10: Which of the following is an odd number?

A) 101 ² + 9	$B)102^2 + 3$
C) $102^2 + 8$	D) 105 ² + 5

Solution: Odd number + even numbe	r = odd number
$B)102^2 + 3 \Longrightarrow Even + Odd = Odd$	Answer: E
Q11: $\frac{4}{0.2} - (0.25)^2 + 1 = ?$	
A) $\frac{289}{16}$ B) $\frac{331}{16}$ C) $\frac{333}{16}$	D) $\frac{337}{16}$
Solution: $4 (1)^2$	
$\frac{1}{0.2} - (0.25)^2 + 1 = 4 \times \frac{10}{2} - (\frac{1}{4}) + 1$	
$\Rightarrow 20 - \frac{1}{16} + 1 = \frac{320 - 1 + 16}{16} = \frac{335}{16}$	
	Answer: 0
Q12: $\left(\frac{3}{7}\right)^3 = ?$	
A) $\frac{27}{7}$ B) $\frac{9}{21}$ C) $\frac{27}{342}$	D) $\frac{33}{343}$
Solution: $\left(\frac{3}{7}\right)^3 = \frac{27}{343}$	
(7) 515	Answor: C

Q13:
$$x - \left[x + \frac{1}{x} \right] + \frac{1}{x} = ?$$

A) 0 B) $2x$ C) $\frac{x+1}{x}$ D) $\frac{1}{x}$

Solution: $x - \left[x + \frac{1}{x} \right] + \frac{1}{x} = x - x - \frac{1}{x} + \frac{1}{x} = 0$ **Answer: A**

Q14: What will be replaced with the question mark in the following equation?

A) 61 B) 24 C) 36 D) 42



Q15: If the average of "a" and "b" is 12 and the average of "c" and "d" is 13 then which of the following is false?

A) a+b=24B) c+d=26C) (c+d)-(a+b)=0D) a+b+c+d=50

Solution: $\frac{a+b}{2} = 12 \Rightarrow a+b = 24, \frac{c+d}{2} = 13 \Rightarrow c+d = 26$ a+b+c+d = 24+26 = 50

Answer: C

Q16: What is the H.C.F. of a and b if both a and b

A)
$$a+b$$
 B) $\frac{a}{b}$ C) $a \times b$ D) 1

Solution: the H.C.F. of a and b if both a and b are prime numbers is 1.

Answer: D

$$5 \triangle 3 = 10$$

Q17:
$$6 \triangle 7 = 37$$

$$8 \triangle 2 = 11$$

$$9 \triangle 11 = ?$$

are prime numbers?

A) 94 B) 88 C) 83 D) 81

Solution:	
$5 \triangle 3 = 10 \Longrightarrow 5 \times 3 - 5 = 15 - 5 = 10$	
$6 \vartriangle 7 = 37 \Longrightarrow 6 \times 7 - 5 = 42 - 5 = 37$	
$8 \vartriangle 2 = 11 \Longrightarrow 8 \times 2 - 5 = 16 - 5 = 11$	
$9 \triangle 11 = ? \Longrightarrow 9 \times 11 - 5 = 99 - 5 = 94$	
	Answer: A

Q18: The average of three numbers is m. What will be the average of the numbers if each of them is increased by 12?

A) 12 <i>m</i>	B) <i>m</i> +12
C) <i>m</i>	D) <i>m</i> -12



Q19: If
$$\frac{4}{5} = \frac{p}{15}$$
 and $\frac{4}{5} = \frac{20}{m}$, what is the value of $p+m2$
 Q22: Which of the following proportions is different than others?

 A) 32
 B) 34
 C) 37
 D) 41

 Solution: $\frac{4}{5} = \frac{2}{2m} \Rightarrow 4m = 100 \Rightarrow m = 25$
 $m = 4$
 B) $m: n = 1: 4 \Rightarrow \frac{m}{n} = \frac{1}{4} \Rightarrow m = 4n$
 $p+m = 12 + 25 = 37$
 Answer: C

 Q20: If $\left(\frac{a}{b}\right)^3 = 4$, what is the value of $\left(\frac{b}{a}\right)^4$?
 Answer: C

 Q21: If $\left(\frac{a}{b}\right)^3 = 4$, what is the value of $\left(\frac{b}{a}\right)^4$?
 Answer: D

 Q21: What is the value of x if $\frac{3x}{2} + \frac{5}{4} = \frac{9}{2} + \frac{x}{2}$?
 A) $\frac{3}{4}$
 B) $\frac{7}{4}$
 D) $\frac{13}{4}$

 Q21: What is the value of x if $\frac{3x}{2} + \frac{5}{4} = \frac{9}{2} + \frac{x}{2}$?
 A) $\frac{3}{4}$
 B) $\frac{7}{4}$
 C) $\frac{14}{4}$
 D) $\frac{13}{4}$

 Q21: What is the value of x if $\frac{3x}{2} + \frac{5}{4} = \frac{9}{2} + \frac{x}{2}$?
 A) $\frac{3}{4}$
 B) $\frac{7}{4}$
 C) $\frac{14}{4}$
 D) $\frac{13}{4}$

 Q21: What is the value of x if $\frac{3x}{2} + \frac{5}{4} = \frac{9}{2} + \frac{x}{2}$
 Q24: If $\sqrt{x} = 12$, what is the value of x?
 A) 12
 B) 24
 C) 144
 D) 136

 Solution: $(5x + 5 = 2(9 + x) \Rightarrow 6x + 5 = 18 + 2x$
 Answer: D
 Answer: C
 Answer: C

Q25: If 25% of *A* is equal to 1200, what is 40% of A + 400?

A) 98 B) 245

Solution:

C) 280

 $\frac{25}{100}A = 1200 \Rightarrow \frac{1}{4}A = 1200 \Rightarrow A = 4800$ $\frac{40}{100}(A + 400) = \frac{40}{100}(4800 + 400) = \frac{40}{100} \times 5200 = 2080$

Answer: D

D) 2080

Q26:
$$\sqrt{0.01} \left(\sqrt{0.36} + \sqrt{0.16} \right) = ?$$

B) 1

A) $\frac{1}{10}$

C)
$$\frac{1}{\sqrt{10}}$$
 D) $\sqrt{10}$

Solution: $\sqrt{0.01} \left(\sqrt{0.36} + \sqrt{0.16} \right) = 0.1 (0.6 + 0.4) = 0.1 \times 1 = \frac{1}{10}$ Answer: A

Q27: If 11 more than m is 7 less than n, what is m in terms of n?

A) *n*+7 B) *n*-7 C) *n*-18 D) *n*-11

Solution: $11+m=n-7 \Rightarrow m=n-7-11=n-18$ Answer: C **Q28:** Usman had an appointment which is 60 km away from his home at 11:00 a.m. He travelled with an average speed of 80 km/h for the trip and arrived 25 minutes late for the appointment. At what time did he leave his home?

A) 09:40 a.m. B) 10:35 a.m.

<mark>C) 10:40 a.m.</mark> I

D) 10:45 a.m.

Solution: $time = \frac{60}{80} \times 60 = \frac{3600}{80} = 45 \min$	I
(11:25)-45==10:40 a.m.	
	Answor: C

Q29: The sum of the squares of which of the following pairs is the greatest?

A) 3 and 6	B) 4 and 5
C) 2 and 7	<mark>D) 8 and 1</mark>

Solution: A) $3^2 + 6^2 = 9 + 36 = 45$ B) $4^2 + 5^2 = 16 + 25 = 41$ C) $2^2 + 7^2 = 4 + 49 = 53$ D) $8^2 + 1^2 = 64 + 1 = 65$ Answer: D

$$\frac{1}{a} + \frac{1}{b} = 15$$
Q30: If $\frac{1}{b} + \frac{1}{c} = 17$ then what is the value of c?
 $\frac{1}{a} + \frac{1}{c} = 12$
A) $\frac{1}{13}$
B) $\frac{1}{10}$
C) $\frac{1}{7}$
D) $\frac{1}{6}$

Solution:

$$2\left(\frac{1}{a} + \frac{1}{b} + \frac{1}{c}\right) = 15 + 17 + 12 \Rightarrow \frac{1}{a} + \frac{1}{b} + \frac{1}{c} = \frac{44}{2} = 22$$

$$\frac{1}{a} + \frac{1}{b} + \frac{1}{c} = 15 + \frac{1}{c} = 22 \Rightarrow \frac{1}{c} = 22 - 15 = 7 \Rightarrow c = \frac{1}{7}$$
Answer: C

A) -3250	B) -800
<mark>C) 800</mark>	D) 3250

Solution:
$$(-45)^2 - 35^2 = 2025 - 1225 = 800$$

Q32:
$$2\sqrt{21-\sqrt{23}+\sqrt{4}} = ?$$

A) 8 B) 6 C) 12

Solution: $2\sqrt{21 - \sqrt{23 + \sqrt{4}}} = 2\sqrt{21 - \sqrt{25}} = 2\sqrt{21 - 5}$ $\Rightarrow 2\sqrt{16} = 2 \times 4 = 8$

Answer: A

D) 10

Q33: Which of the following three numbers whose products should be multiplied by 24 to get a perfect square?

A) 1, 2 and 3 C) 1, 3 and 5 B) 2, 3 and 5 D) 3, 5 and 6

Solution: $24 \times 1 \times 2 \times 3 = 144 = 12^2$

Answer: A

Q34: 8 workers can paint a building in 27 days. How many days will it take 18 workers to paint the same building?

Solution:
$$x = \frac{8 \times 27}{18} = 4 \times 3 = 12$$

Answer: B

Q35: If $a^2b = 12^2$ and *b* is an integer, then *a* is not divisible by _____.

A) 3 B) 4 C) 6 D) 8

Solution: $a^2b = 12^2 \times 1 \Rightarrow a = 12 \Rightarrow 12$ is not divisible by 8 Answer: D

Q36: Which of the following problems cannot be solved by using the equation 5x-7 = x+17?

I. 7 less than 5 times a certain number is equal to 17 more than the number. What is the number?

II. The age of Hassan after 17 years will be 7 less than 5 times his present age. What is his age?

III. 5 times 7 less than a certain number is equal to17 more than the same number. What is the number?

A) Only I	B) I and II
C) II and III	D) Only III

Solution: III. 5 times 7 less than a certain number is equal to 17 more than the same number. What is the number? $\Rightarrow 7-5x = x+17$

Answer: D

Q37: What is the number of all possible triangles drawn in the figure given below?



Solution: Count all possible no. of triangles.
Answer: B

Q38: The shaded areas in the figures given below are removed. Which shape has the longest perimeter after the shaded parts are removed?



Q39: What is the area of the triangle KLM if its height is 42 cm?



Solution:	
area of the triangle KLM = $\frac{42 \times 70}{2} = 21$	$\times 70 = 1470$
	Answer: B

Q40: In the figure below, the perimeter of the rectangle *ABCD* is 40 cm and the perimeter of the rectangle *CDEF* is 32 cm. What is the perimeter of the rectangle *ABEF* if the length of the side *CD* is 7 cm?



D) 72 cm

Solution:

<mark>A) 58 cm</mark>

the perimeter of the rectangle ABEF = $40 + 32 - 2 \times 7$ $\Rightarrow 72 - 14 = 58cm$

Answer: A

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Q41: The net of a cube with numbered faces is shown in the diagram.



Urva correctly adds the numbers on opposite faces of this cube. Which sums does Urva get?

A) 4, 7 and 10 C) 7, 7 and 7 B) 8, 9 and 4 D) 6, 8 and 10

Solution: Opposite faces are: 1+3=4, 2+5=7, 4+6=10

Answer: A

Q42: If 360 of the owners got their cat from a shelter, how many of the owners got their cat from friends according to pie chart?



Solution:
$$\frac{360}{F} = \frac{24}{45} \Rightarrow F = \frac{360 \times 45}{24} = 675$$

Answer: D

We believe what is taught with love lasts forever

Q43: Find the value of x if
$$4 + \frac{12}{2 - \frac{3}{\frac{2 - x}{2}}} = 8$$

A) 8 B) 6 C) -6 D) -8



Q44: Each of 9 students conducted an experiment, and the average time for the 9 experiments was 34 minutes. If the average time for 5 of the experiments was 30 minutes, what was the average time, in minutes, for the other 4 experiments?

A) 38	B) 38.5	C) 39	D) 39.5
	D) 00.0	<u> </u>	2,000

Solution: average time for 4 experiments= $\frac{9 \times 34 - 5 \times 30}{4}$ $\frac{306 - 150}{4} = \frac{156}{4} = 39$ Answer: C

Q45: In the following circle with centre O, the shaded area represents 25% of the area of the circle. What is the size of angle AOB?



Q46: What is the unknown number indicated by question mark?



A) 7 B) 14 C) 21 D) 42

Solution: $2 \times ? = 14 \Longrightarrow ? = \frac{14}{2} = 7$ Answer: A

Q47: The perimeter of the $\triangle ABC$ below is 82 cm. What is the value of x?





Q48: In the figure below, a rectangular prism and its net is given. Which letter will be X?





Q49: According to the given table below, numbers are increasing by double from left to right and decreasing by half top to down. What is the value of K-L?



Q50: x, y and z are three digits.

What is the value of x + y + z according to subtraction?

A) 13 B) 15 C) 17 D) 19

Solution: x + y + z = 6 + 9 + 2 = 17

Answer: C